

Quality test for Relational DBs

Reading: Elmasri & Navathe, Fundamentals of
Database Systems, Chapter 14.

Recap: Normal Forms

- Based on functional dependencies:
 - 1st Normal Form (1NF)
 - 2nd Normal Form (2NF)
 - 3rd Normal Form (3NF)
 - Boyce-Codd Normal Form (BCNF)
- Based on “multivalued” and “join” dependencies:
 - 4th and 5th Normal Forms (4NF, 5NF)
- Each NF extends the previous (so a relation in 3NF is also in 2NF and 1NF)

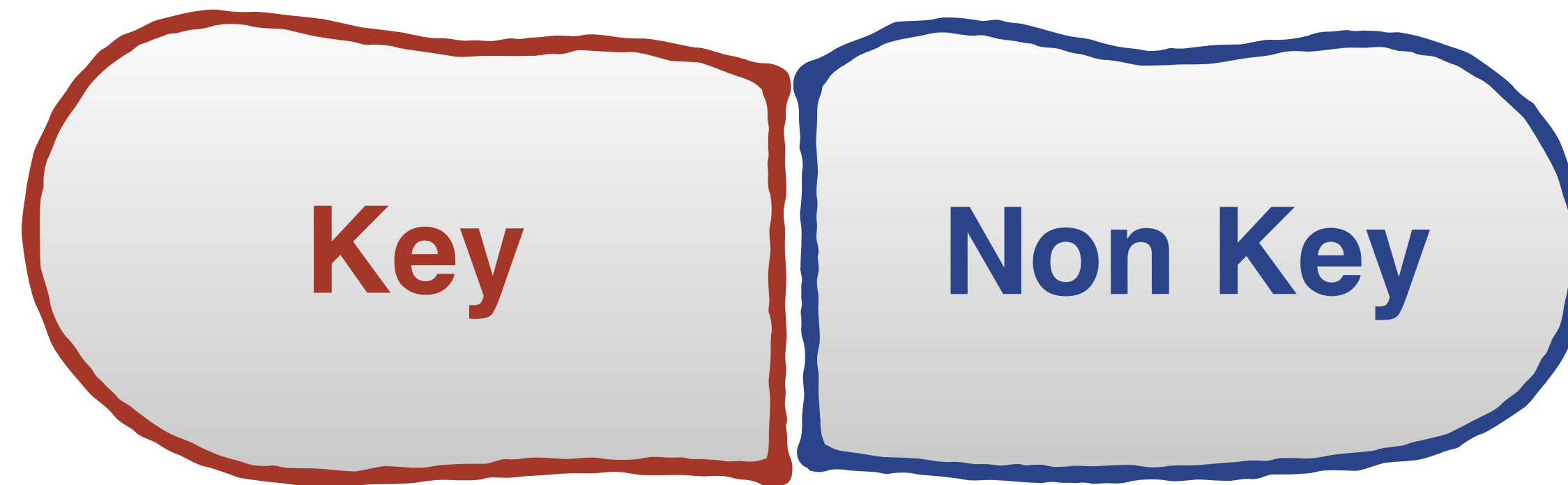
A graphic guide to FD based Normal Forms

consider Your Typical Relation:

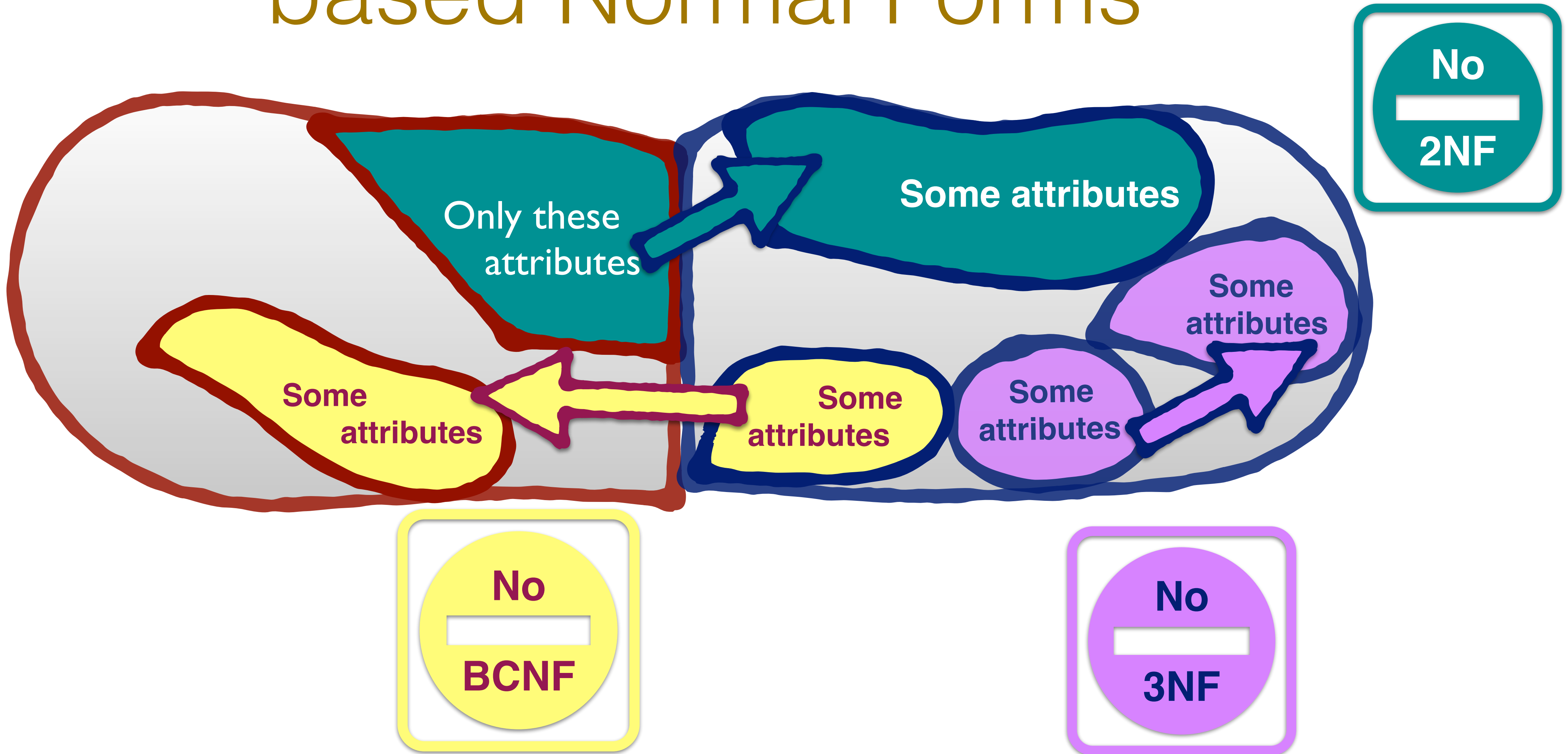
YTR = {**KeyAtt1, KeyAtt2,...KeyAttN**, NonKeyAtt1,.....NonKeyAttM}

| KeyAtt1 | KeyAttN | NonKeyAtt1 | NonKeyAttM |
|---------|-----------------|------------|------------|
| 534563 | gdfg | 46gr34 | 234wfwf |
| 534563 | gdfg | 46gr34 | 234wfwf |
| 534563 | Some data in... | 46gr34 | fwer5wwf |
| 534563 | gdfgd | g4t3463 | 35rwwet5 |
| 583240 | urtr | g3463g3 | fwty4rwwg |

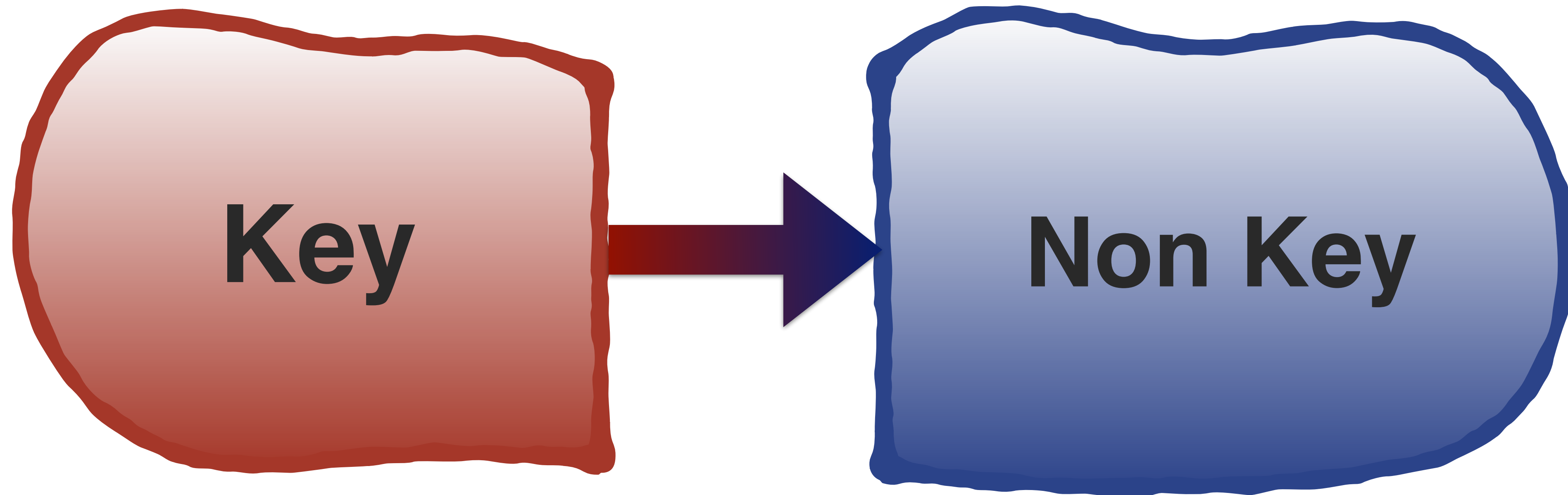
A graphic guide to FD based Normal Forms



A graphic guide to FD based Normal Forms



BCNF (and 3NF, and 2NF)



1. The whole key is needed to determine ALL non key attributes.
2. There are **NO OTHER dependencies**.

Normal Forms: not enough

- When considered in isolation, NFs do not guarantee a good design
- Important additional properties to check:
 - **Dependency preservation property:** Each functional dependency is represented in some relation after normalisation. Desirable but can be sacrificed for other factors.
 - **Non-additive join property:** No spurious tuples are generated after normalisation. Extremely critical.
- Algorithms can be used to guarantee that a set of relations satisfies either or both of the properties above

REMEMBER OUR PROBLEMATIC TABLE?

Students

| StudentID | Department | Tutor |
|-----------|------------|----------|
| 123 | Physics | Einstein |
| 123 | Music | Mozart |
| 456 | Biology | Darwin |
| 789 | Physics | Bohr |
| 999 | Physics | Einstein |

- this was non BCNF
- 3 alternative solutions
- let's test them all

1.

| StudentID | Tutor |
|-----------|----------|
| 123 | Einstein |
| 123 | Mozart |
| 456 | Darwin |
| 789 | Bohr |
| 999 | Einstein |

| StudentID | Department |
|-----------|------------|
| 123 | Physics |
| 123 | Music |
| 456 | Biology |
| 789 | Physics |
| 999 | Physics |

2.

| Tutor | Department |
|----------|------------|
| Einstein | Physics |
| Mozart | Music |
| Darwin | Biology |
| Bohr | Physics |

| StudentID | Department |
|-----------|------------|
| 123 | Physics |
| 123 | Music |
| 456 | Biology |
| 789 | Physics |
| 999 | Physics |

3.

| Tutor | Department |
|----------|------------|
| Einstein | Physics |
| Mozart | Music |
| Darwin | Biology |
| Bohr | Physics |

| StudentID | Tutor |
|-----------|----------|
| 123 | Einstein |
| 123 | Mozart |
| 456 | Darwin |
| 789 | Bohr |
| 999 | Einstein |

Dependency preservation

Students

| StudentID | Department | Tutor |
|-----------|------------|----------|
| 123 | Physics | Einstein |
| 123 | Music | Mozart |
| 456 | Biology | Darwin |
| 789 | Physics | Bohr |
| 999 | Physics | Einstein |

- Functional Dependencies:
 1. $\{StudentID, Department\} \rightarrow Tutor$
 2. $Tutor \rightarrow Department$

3.

| Tutor | Department |
|----------|------------|
| Einstein | Physics |
| Mozart | Music |
| Darwin | Biology |
| Bohr | Physics |

| StudentID | Tutor |
|-----------|----------|
| 123 | Einstein |
| 123 | Mozart |
| 456 | Darwin |
| 789 | Bohr |
| 999 | Einstein |

- This set of tables is BCNF
- However: Functional Dependency 1. is **not** preserved
- There is no way we can tell it holds

Non-additive join

1.

| StudentID | Tutor | StudentID | Department |
|-----------|----------|-----------|------------|
| 123 | Einstein | 123 | Physics |
| 123 | Mozart | 123 | Music |
| 456 | Darwin | 456 | Biology |
| 789 | Bohr | 789 | Physics |
| 999 | Einstein | 999 | Physics |

This BCNF decomposition does not have the **non-additive join property** as spurious tuples can be produced

R1 join R2 =

| StudentID | Department | Tutor |
|-----------|------------|----------|
| 123 | Physics | Einstein |
| 123 | Music | Mozart |
| 123 | Physics | Mozart |
| 123 | Music | Einstein |
| 456 | Biology | Darwin |
| 789 | Physics | Bohr |
| 999 | Physics | Einstein |

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Students

| StudentID | Department | Tutor |
|-----------|------------|----------|
| 123 | Physics | Einstein |
| 123 | Music | Mozart |
| 456 | Biology | Darwin |
| 789 | Physics | Bohr |
| 999 | Physics | Einstein |

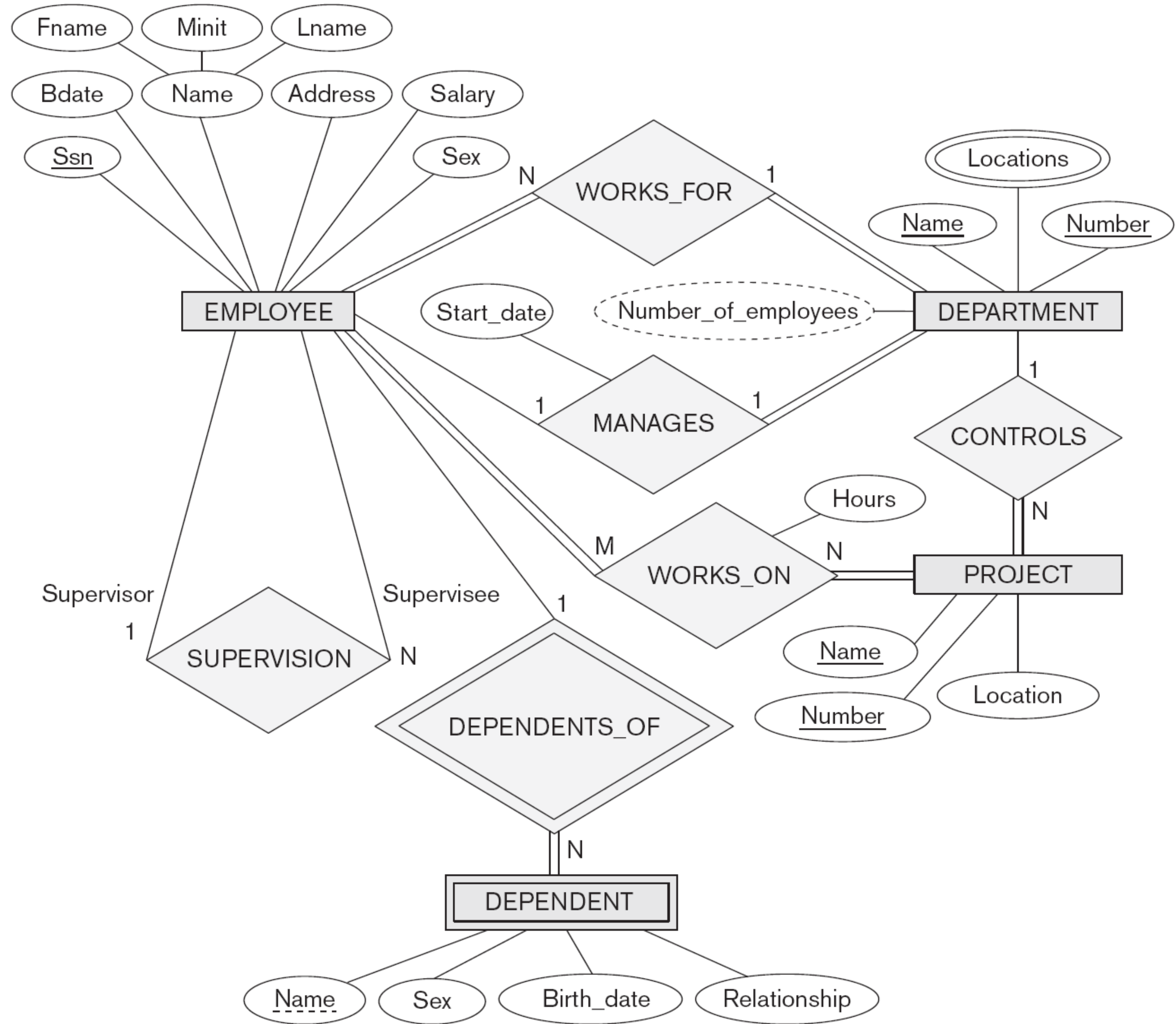
Testing for non-additive join

- Problem: relying on finding examples is not the best strategy
- We need a more systematic procedure
- **“Tableaux test for non-additive join”**
 - starting from the “universal relation” and the set of FDs
 - gives an algorithm for easy checking
 - if the test succeeds, we can be sure ALL instances of the database will never generate spurious tuples
 - if the test fails, it also gives the counterexample we need

Tableaux test

- Principle: simulate what would happen if a report was created that joined *all tables* in the database
- One would assume that only very few individuals are such that their relationships can be traced through *all* tables
- If a join over all tables produced a potentially infinite amount of such individuals, we would be in the presence of spurious records
- We would like to test this, without having to populate the database with 1000s of records in the hope of finding a good example by chance

In the company example, this would mean to search for all employees **who** work for a department, **and** manage a department, **and** work on a project, **which is** controlled by a department, **and** have a supervisor, **and** have a dependent.



We can simulate this by building a table containing **ALL** attributes of the database (the “Universal Relation”) and **one row for each** table (relation) of the DB, and filling it in with generic values, arbitrary, **but constrained by the functional dependencies**

| | Attribute 1 | Attribute 2 | ... | ... | ... | Attribute N |
|------------|-------------|-------------|-----|-----|-----|-------------|
| Relation 1 | | | | | | |
| Relation 2 | | | | | | |
| ... | | | | | | |
| ... | | | | | | |
| Relation M | | | | | | |

Let's test our example

3.

| Tutor | Department | StudentID | Tutor |
|----------|------------|-----------|----------|
| Einstein | Physics | 123 | Einstein |
| Mozart | Music | 123 | Mozart |
| Darwin | Biology | 456 | Darwin |
| Bohr | Physics | 789 | Bohr |
| | | 999 | Einstein |

- The Universal relation is {StudentID, Tutor, Department}
- The Relations are $R1 = \{\text{Tutor, Department}\}$ and $R2 = \{\text{StudentID, Tutor}\}$
- The only functional dependency that we can represent here is $\text{Tutor} \rightarrow \text{Department}$

- Universal relation {StudentID, Tutor, Department}
- $R_1 = \{\text{Tutor, Department}\}$ and $R_2 = \{\text{StudentID, Tutor}\}$
- FD: Tutor \rightarrow Department

1. Prepare the table:


| | StudentID | Tutor | Department |
|-------|-----------|-------|------------|
| R_1 | | | |
| R_2 | | | |

- Universal relation {StudentID, Tutor, Department}
- • R1={Tutor, Department} and R2={StudentID, Tutor}
- FD: Tutor → Department

2. Fill each row with generic values, ensuring consistency:


We use each relation in turn and add values to “activated” attributes in each row

| | StudentID | Tutor | Department |
|------------------|-----------|---------|------------|
| → R ₁ | | Value 1 | Value 2 |
| R ₂ | | | |

- Universal relation {StudentID, Tutor, Department}
- R1={Tutor, Department} and
 R2={StudentID, Tutor}
- FD: Tutor \rightarrow Department

2. Fill each row with generic values, ensuring consistency:

We use each relation in turn and add values to “activated” attributes in each row




| | StudentID | Tutor | Department |
|----------------|-----------|---------|------------|
| R ₁ | | Value 1 | Value 2 |
| R ₂ | Value 3 | Value 1 | |

- Universal relation {StudentID, Tutor, Department}
- $R_1 = \{\text{Tutor, Department}\}$ and $R_2 = \{\text{StudentID, Tutor}\}$
- FD: Tutor \rightarrow Department

2. Fill each row with generic values, ensuring consistency:



We use each relation in turn and add values to “activated” attributes in each row

| | StudentID | Tutor | Department |
|-------|-----------|---------|------------|
| R_1 | | Value 1 | Value 2 |
| R_2 | Value 3 | Value 1 | |

- Universal relation {StudentID, Tutor, Department}
- $R_1 = \{\text{Tutor, Department}\}$ and $R_2 = \{\text{StudentID, Tutor}\}$
- FD: Tutor \rightarrow Department


“All tuples with same Tutor must have the same Department”

3. Apply the Functional Dependencies in turn

| | StudentID | Tutor | Department |
|---|-----------|---------|------------|
|  R_1 | | Value 1 | Value 2 |
|  R_2 | Value 3 | Value 1 | Value 2 |

- Universal relation {StudentID, Tutor, Department}
- $R_1 = \{\text{Tutor, Department}\}$ and $R_2 = \{\text{StudentID, Tutor}\}$
- FD: Tutor \rightarrow Department

If we manage to complete a row of values, we pass the test!

| | StudentID | Tutor | Department |
|-------|-----------|---------|------------|
| R_1 | | Value 1 | Value 2 |
| R_2 | Value 3 | Value 1 | Value 2 |

- Universal relation {StudentID, Tutor, Department}
- $R_1 = \{\text{Tutor, Department}\}$ and $R_2 = \{\text{StudentID, Tutor}\}$
- FD: Tutor \rightarrow Department

If we manage to complete a row of values, we pass the test!

This DB is safe from producing spurious records



| | StudentID | Tutor | Department |
|-------|-----------|---------|------------|
| R_1 | | Value 1 | Value 2 |
| R_2 | Value 3 | Value 1 | Value 2 |

Let's test another example

2.

| Tutor | Department | StudentID | Department |
|----------|------------|-----------|------------|
| Einstein | Physics | 123 | Physics |
| Mozart | Music | 123 | Music |
| Darwin | Biology | 456 | Biology |
| Bohr | Physics | 789 | Physics |
| | | 999 | Physics |

- The Universal relation is {StudentID, Tutor, Department}
- The Relations are $R1 = \{\text{Tutor, Department}\}$ and $R2 = \{\text{StudentID, Department}\}$
- The functional dependency that we can represent here is only:
Tutor \rightarrow Department

- Universal relation {StudentID, Tutor, Department}
- $R_1 = \{\text{Tutor, Department}\}$ and $R_2 = \{\text{StudentID, Department}\}$
- FD: Tutor \rightarrow Department

1. Prepare the table:

| | StudentID | Tutor | Department |
|-------|-----------|-------|------------|
| R_1 | | | |
| R_2 | | | |


- Universal relation {StudentID, Tutor, Department}
- • R1={Tutor, Department} and R2={StudentID, Department}
- FD: Tutor → Department

2. Fill each row with generic values, ensuring consistency:

| | StudentID | Tutor | Department |
|------------------|-----------|---------|------------|
| → R ₁ | | Value 1 | Value 2 |
| R ₂ | | | |

- Universal relation {StudentID, Tutor, Department}
- R1={Tutor, Department} and
 R2={StudentID, Department}
- FD: Tutor \rightarrow Department

2. Fill each row with generic values, ensuring consistency:




| | StudentID | Tutor | Department |
|----------------|-----------|---------|------------|
| R ₁ | | Value 1 | Value 2 |
| R ₂ | Value 3 | | Value 2 |

- Universal relation {StudentID, Tutor, Department}
- $R_1 = \{\text{Tutor, Department}\}$ and $R_2 = \{\text{StudentID, Department}\}$
- FD: Tutor \rightarrow Department


2. Fill each row with generic values, ensuring consistency:

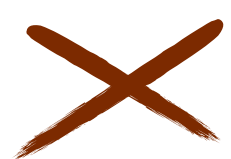
| | StudentID | Tutor | Department |
|-------|-----------|---------|------------|
| R_1 | | Value 1 | Value 2 |
| R_2 | Value 3 | | Value 2 |

- Universal relation {StudentID, Tutor, Department}
- $R_1 = \{\text{Tutor, Department}\}$ and $R_2 = \{\text{StudentID, Department}\}$
- FD: Tutor \rightarrow Department


“All tuples with same Tutor must have the same Department”

3. Apply the Functional Dependencies in turn



| | StudentID | Tutor | Department |
|-------|-----------|---|------------|
| R_1 | | Value 1 | Value 2 |
| R_2 | Value 3 |  | Value 2 |

- Universal relation {StudentID, Tutor, Department}
- $R_1 = \{\text{Tutor, Department}\}$ and $R_2 = \{\text{StudentID, Department}\}$
- FD: Tutor ~~\rightarrow~~ Department

There are no 2 tuples where we can apply this FD

3. Apply the Functional Dependencies in turn

| | StudentID | Tutor | Department |
|-------|-----------|---------|------------|
| R_1 | | Value 1 | Value 2 |
| R_2 | Value 3 | | Value 2 |

- Universal relation {StudentID, Tutor, Department}
- $R_1 = \{\text{Tutor, Department}\}$ and $R_2 = \{\text{StudentID, Department}\}$
- FD: Tutor ~~\rightarrow~~ Department

There are no 2 tuples where we can apply this FD

If we manage to complete a row of values, we pass the test!

This DB could produce spurious records



| | StudentID | Tutor | Department |
|-------|-----------|---------|------------|
| R_1 | | Value 1 | Value 2 |
| R_2 | Value 3 | | Value 2 |

The final table can be used as counterexample: let's fill it in with more meaningful values

| | StudentID | Tutor | Department |
|-------|-----------|---------|------------|
| R_1 | | Value 1 | Value 2 |
| R_2 | Value 3 | | Value 2 |

The final table can be used as counterexample: let's fill it in with more meaningful values

| | StudentID | Tutor | Department |
|-------|-----------|---------|------------|
| R_1 | | Value 1 | CompSci |
| R_2 | Value 3 | | CompSci |

The final table can be used as counterexample: let's fill it in with more meaningful values

| | StudentID | Tutor | Department |
|-------|-----------|--------|------------|
| R_1 | | Turing | CompSci |
| R_2 | Value 3 | Hopper | CompSci |

The final table can be used as counterexample: let's fill it in with more meaningful values

| StudentID | Tutor | Department |
|-----------|--------|------------|
| St1 | Turing | CompSci |
| St2 | Hopper | CompSci |

$R1 = \{\text{Tutor, Department}\}$

| Tutor | Department |
|--------|------------|
| Turing | CompSci |
| Hopper | CompSci |

$R2 = \{\text{StudentID, Department}\}$

| StudentID | Department |
|-----------|------------|
| St1 | CompSci |
| St2 | CompSci |

| StudentID | Department |
|-----------|------------|
| St1 | CompSci |
| St2 | CompSci |

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| Tutor | Department |
|--------|------------|
| Turing | CompSci |
| Hopper | CompSci |

=

| StudentID | Department | Tutor |
|-----------|--------------------|--------|
| St1 | CompSci | Turing |
| St2 | CompSci | Turing |
| St1 | CompSci | Hopper |
| St2 | CompSci | Hopper |

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| StudentID | Tutor | Department |
|-----------|--------|------------|
| St1 | Turing | CompSci |
| St2 | Hopper | CompSci |

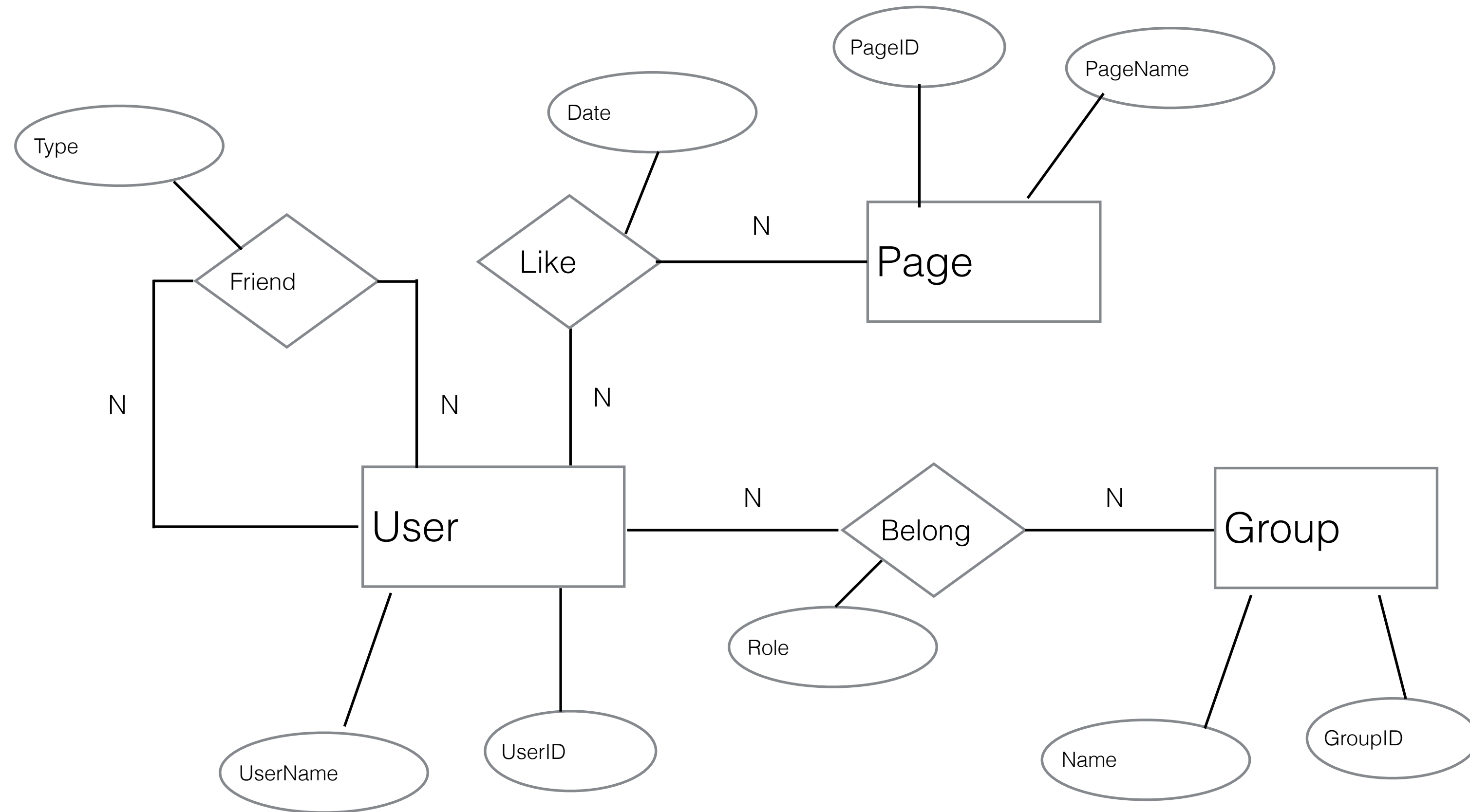
What about solution 1?

1.

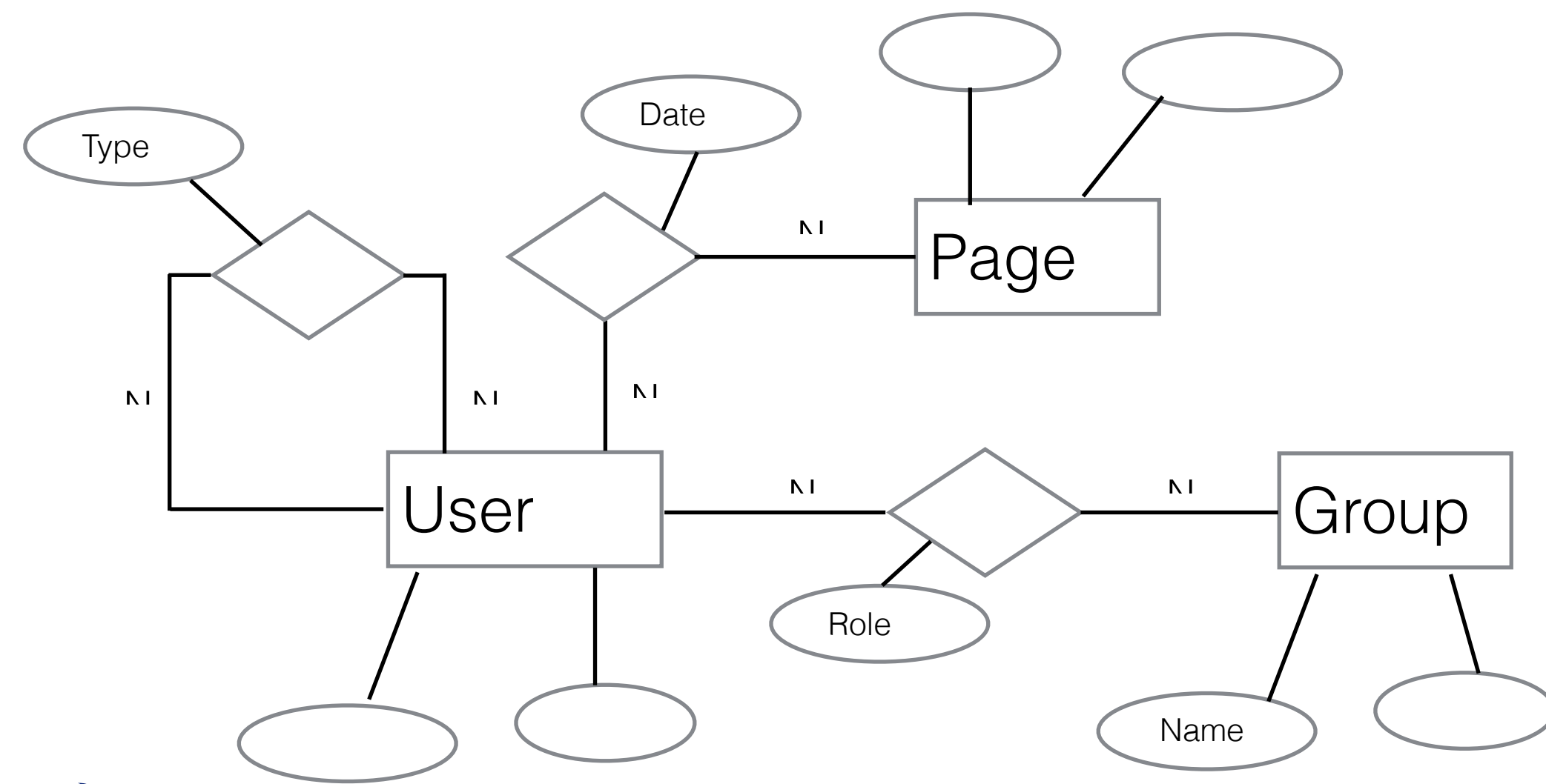
| StudentID | Tutor | StudentID | Department |
|-----------|----------|-----------|------------|
| 123 | Einstein | 123 | Physics |
| 123 | Mozart | 123 | Music |
| 456 | Darwin | 456 | Biology |
| 789 | Bohr | 789 | Physics |
| 999 | Einstein | 999 | Physics |

- The Universal relation is {StudentID, Tutor, Department}
- The Relations are $R1=\{StudentID, Tutor\}$ and $R2=\{StudentID, Department\}$
- The functional dependencies that we can represent here are...
 - NONE!
- The decomposition fails the test immediately

No design is waterproof!

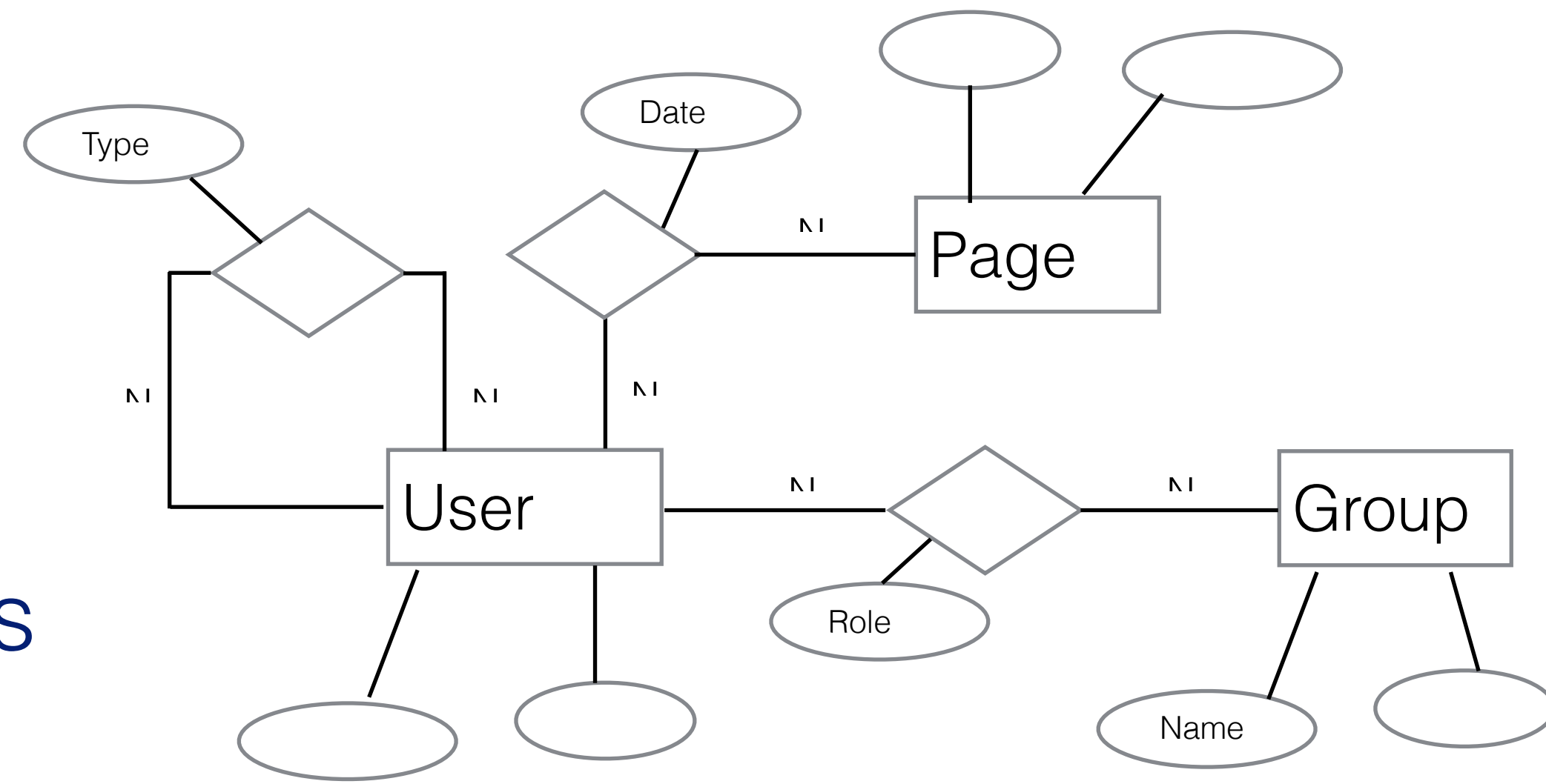


A simplified social network!



Relations:

- $R1 = \{\underline{\text{UserID}}, \text{Username}\}$
- $R2 = \{\underline{\text{GroupID}}, \text{GroupName}\}$
- $R3 = \{\underline{\text{PageID}}, \text{PageName}\}$
- $R4 = \{\underline{\text{UserID}}, \underline{\text{PageID}}, \text{Date}\}$ (*user likes page*)
- $R5 = \{\underline{\text{UserID}}, \underline{\text{GroupID}}, \text{Role}\}$ (*user belongs to group*)
- $R6 = \{\underline{\text{UserID}}, \underline{\text{FriendID}}, \text{Type}\}$ (*user friends user*)



Functional dependencies

- $UserID \rightarrow Username$
- $GroupID \rightarrow GroupName$
- $PageID \rightarrow PageName$
- $\{UserID, PageID\} \rightarrow Date$
- $\{UserID, GroupID\} \rightarrow Role$
- $\{UserID, FriendID\} \rightarrow Type$

- BCNF set of tables
- and we also can preserve all dependencies

The Tableaux test

- Construct the rows, one for each relation:

| | UserID | Username | GroupID | GroupName | PageID | PageName | Date | Role | FriendID | Type |
|----|--------|----------|---------|-----------|--------|----------|--------|--------|----------|---------|
| R1 | Value1 | Value2 | | | | | | | | |
| R2 | | | Value3 | Value4 | | | | | | |
| R3 | | | | | Value5 | Value6 | | | | |
| R4 | Value1 | | | | Value5 | | Value7 | | | |
| R5 | Value1 | | Value3 | | | | | Value8 | | |
| R6 | Value1 | | | | | | | | Value9 | Value10 |

The Tableaux test

- *UserID* → *Username*

| | UserID | Username | GroupID | GroupName | PageID | PageName | Date | Role | FriendID | Type |
|----|--------|----------|---------|-----------|--------|----------|--------|--------|----------|---------|
| R1 | Value1 | Value2 | | | | | | | | |
| R2 | | | Value3 | Value4 | | | | | | |
| R3 | | | | | Value5 | Value6 | | | | |
| R4 | Value1 | | | | Value5 | | Value7 | | | |
| R5 | Value1 | | Value3 | | | | | Value8 | | |
| R6 | Value1 | | | | | | | | Value9 | Value10 |

The Tableaux test

- *UserID* → *Username*

| | UserID | Username | GroupID | GroupName | PageID | PageName | Date | Role | FriendID | Type |
|----|--------|----------|---------|-----------|--------|----------|--------|--------|----------|---------|
| R1 | Value1 | Value2 | | | | | | | | |
| R2 | | | Value3 | Value4 | | | | | | |
| R3 | | | | | Value5 | Value6 | | | | |
| R4 | Value1 | Value2 | | | Value5 | | Value7 | | | |
| R5 | Value1 | Value2 | Value3 | | | | | Value8 | | |
| R6 | Value1 | Value2 | | | | | | | Value9 | Value10 |

The Tableaux test

- *GroupID* → *GroupName*

| | UserID | Username | GroupID | GroupName | PageID | PageName | Date | Role | FriendID | Type |
|----|--------|----------|---------|-----------|--------|----------|--------|--------|----------|---------|
| R1 | Value1 | Value2 | | | | | | | | |
| R2 | | | Value3 | Value4 | | | | | | |
| R3 | | | | | Value5 | Value6 | | | | |
| R4 | Value1 | Value2 | | | Value5 | | Value7 | | | |
| R5 | Value1 | Value2 | Value3 | | | | | Value8 | | |
| R6 | Value1 | Value2 | | | | | | | Value9 | Value10 |

The Tableaux test

- *GroupID* → *GroupName*

| | UserID | Username | GroupID | GroupName | PageID | PageName | Date | Role | FriendID | Type |
|----|--------|----------|---------|-----------|--------|----------|--------|--------|----------|---------|
| R1 | Value1 | Value2 | | | | | | | | |
| R2 | | | Value3 | Value4 | | | | | | |
| R3 | | | | | Value5 | Value6 | | | | |
| R4 | Value1 | Value2 | | | Value5 | | Value7 | | | |
| R5 | Value1 | Value2 | Value3 | Value4 | | | | Value8 | | |
| R6 | Value1 | Value2 | | | | | | | Value9 | Value10 |

The Tableaux test

- *PageID* → *PageName*

| | UserID | Username | GroupID | GroupName | PageID | PageName | Date | Role | FriendID | Type |
|----|--------|----------|---------|-----------|--------|----------|--------|--------|----------|---------|
| R1 | Value1 | Value2 | | | | | | | | |
| R2 | | | Value3 | Value4 | | | | | | |
| R3 | | | | | Value5 | Value6 | | | | |
| R4 | Value1 | Value2 | | | Value5 | | Value7 | | | |
| R5 | Value1 | Value2 | Value3 | Value4 | | | | Value8 | | |
| R6 | Value1 | Value2 | | | | | | | Value9 | Value10 |

The Tableaux test

- *PageID* → *PageName*

| | UserID | Username | GroupID | GroupName | PageID | PageName | Date | Role | FriendID | Type |
|----|--------|----------|---------|-----------|--------|----------|--------|--------|----------|---------|
| R1 | Value1 | Value2 | | | | | | | | |
| R2 | | | Value3 | Value4 | | | | | | |
| R3 | | | | | Value5 | Value6 | | | | |
| R4 | Value1 | Value2 | | | Value5 | Value6 | Value7 | | | |
| R5 | Value1 | Value2 | Value3 | Value4 | | | | Value8 | | |
| R6 | Value1 | Value2 | | | | | | | Value9 | Value10 |

The Tableaux test

- $\{UserID, PageID\} \rightarrow Date$

| | UserID | Username | GroupID | GroupName | PageID | PageName | Date | Role | FriendID | Type |
|----|--------|----------|---------|-----------|--------|----------|--------|--------|----------|---------|
| R1 | Value1 | Value2 | | | ✗ | | | | | |
| R2 | | | Value3 | Value4 | | | | | | |
| R3 | ✗ | | | | Value5 | Value6 | | | | |
| R4 | Value1 | Value2 | | | Value5 | Value6 | Value7 | | | |
| R5 | Value1 | Value2 | Value3 | Value4 | ✗ | | | Value8 | | |
| R6 | Value1 | Value2 | | | ✗ | | | | Value9 | Value10 |

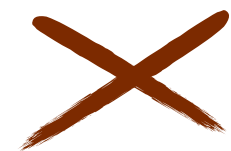
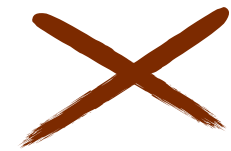
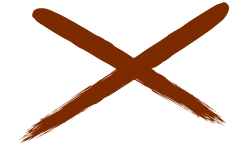
The Tableaux test

- $\{UserID, GroupID\} \rightarrow Role$

| | UserID | Username | GroupID | GroupName | PageID | PageName | Date | Role | FriendID | Type |
|----|--------|----------|---------|-----------|--------|----------|--------|--------|----------|---------|
| R1 | Value1 | Value2 | X | | | | | | | |
| R2 | X | | Value3 | Value4 | | | | | | |
| R3 | | | | | Value5 | Value6 | | | | |
| R4 | Value1 | Value2 | X | | Value5 | Value6 | Value7 | | | |
| R5 | Value1 | Value2 | Value3 | Value4 | | | | Value8 | | |
| R6 | Value1 | Value2 | X | | | | | | Value9 | Value10 |

The Tableaux test

- $\{UserID, FriendID\} \rightarrow Type$

| | UserID | Username | GroupID | GroupName | PageID | PageName | Date | Role | FriendID | Type |
|----|--------|----------|---------|-----------|--------|----------|--------|--------|---|---------|
| R1 | Value1 | Value2 | | | | | | |  | |
| R2 | | | Value3 | Value4 | | | | | | |
| R3 | | | | | Value5 | Value6 | | | | |
| R4 | Value1 | Value2 | | | Value5 | Value6 | Value7 | |  | |
| R5 | Value1 | Value2 | Value3 | Value4 | | | | Value8 |  | |
| R6 | Value1 | Value2 | | | | | | | Value9 | Value10 |

The Tableaux test

This DB could produce spurious records!!!



| | UserID | Username | GroupID | GroupName | PageID | PageName | Date | Role | FriendID | Type |
|----|--------|----------|---------|-----------|--------|----------|--------|--------|----------|---------|
| R1 | Value1 | Value2 | | | | | | | | |
| R2 | | | Value3 | Value4 | | | | | | |
| R3 | | | | | Value5 | Value6 | | | | |
| R4 | Value1 | Value2 | | | Value5 | Value6 | Value7 | | | |
| R5 | Value1 | Value2 | Value3 | Value4 | | | | Value8 | | |
| R6 | Value1 | Value2 | | | | | | | Value9 | Value10 |

The counterexample

| | UserID | Username | GroupID | GroupName | PageID | PageName | Date | Role | FriendID | Type |
|----|--------|----------|---------|-----------|--------|----------|--------|--------|----------|---------|
| R1 | Value1 | Value2 | | | | | | | | |
| R2 | | | Value3 | Value4 | | | | | | |
| R3 | | | | | Value5 | Value6 | | | | |
| R4 | Value1 | Value2 | | | Value5 | Value6 | Value7 | | | |
| R5 | Value1 | Value2 | Value3 | Value4 | | | | Value8 | | |
| R6 | Value1 | Value2 | | | | | | | Value9 | Value10 |

The counterexample

| | UserID | Username | GroupID | GroupName | PageID | PageName | Date | Role | FriendID | Type |
|----|--------|----------|---------|-----------|--------|----------|--------|-----------|----------|------|
| R1 | UI | John | | | | | | | .. | .. |
| R2 | | | GI | Bikers | | | | | .. | .. |
| R3 | | | | | PI | StarWars | | | .. | .. |
| R4 | UI | John | | | PI | StarWars | 1.4.19 | | .. | .. |
| R5 | UI | John | GI | Bikers | | | | Treasurer | .. | .. |
| R6 | UI | John | | | | | | | .. | .. |



Ignore this for brevity

The counterexample

| | UserID | Username | GroupID | GroupName | PageID | PageName | Date | Role | FriendID | Type |
|----|--------|----------|---------|-----------|--------|-----------|--------|-----------|----------|------|
| R1 | U1 | John | G2 | Geeks | P2 | Pizza | 1.1.19 | Admin | .. | .. |
| R2 | U2 | Mary | G1 | Bikers | P3 | Liverpool | 1.2.19 | Owner | .. | .. |
| R3 | U3 | Sarah | G3 | Chefs | P1 | StarWars | 1.3.19 | Fan | .. | .. |
| R4 | U1 | John | G4 | Travel | P1 | StarWars | 1.4.19 | Supporter | .. | .. |
| R5 | U1 | John | G1 | Bikers | P4 | Van Gogh | 1.5.19 | Treasurer | .. | .. |
| R6 | U1 | John | G5 | MovieClub | P5 | Java! | 1.6.19 | Chief | .. | .. |



Ignore this for brevity

| | UserID | Username | GroupID | GroupName | PageID | PageName | Date | Role | Frie | Type |
|----|--------|----------|---------|-----------|--------|-----------|--------|-----------|------|------|
| R1 | U1 | John | G2 | Geeks | P2 | Pizza | 1.1.19 | Admin | .. | .. |
| R2 | U2 | Mary | G1 | Bikers | P3 | Liverpool | 1.2.19 | Owner | .. | .. |
| R3 | U3 | Sarah | G3 | Chefs | P1 | StarWars | 1.3.19 | Fan | .. | .. |
| R4 | U1 | John | G4 | Travel | P1 | StarWars | 1.4.19 | Supporter | .. | .. |
| R5 | U1 | John | G1 | Bikers | P4 | Van Gogh | 1.5.19 | Treasurer | .. | .. |
| R6 | U1 | John | G5 | MovieClub | P5 | Java! | 1.6.19 | Chief | ... | ... |

| UserID | Username |
|--------|----------|
| U1 | John |
| U2 | Mary |
| U3 | Sarah |

| GroupID | GroupName |
|---------|-----------|
| G1 | Bikers |
| G2 | Geeks |
| G3 | Chefs |
| G4 | Travel |
| G5 | MovieClub |

| PageID | PageName |
|--------|-----------|
| P1 | StarWars |
| P2 | Pizza |
| P3 | Liverpool |
| P4 | Van Gogh |
| P5 | Java! |

| UserID | GroupID | Role |
|--------|---------|-----------|
| U1 | G2 | Admin |
| U2 | G1 | Owner |
| U3 | G3 | Fan |
| U1 | G4 | Supporter |
| U1 | G1 | Treasurer |
| U1 | G5 | Chief |

| UserID | PageID | Date |
|--------|--------|--------|
| U1 | P2 | 1.1.19 |
| U2 | P3 | 1.2.19 |
| U3 | P1 | 1.3.19 |
| U1 | P1 | 1.4.19 |
| U1 | P4 | 1.5.19 |
| U1 | P5 | 1.6.19 |

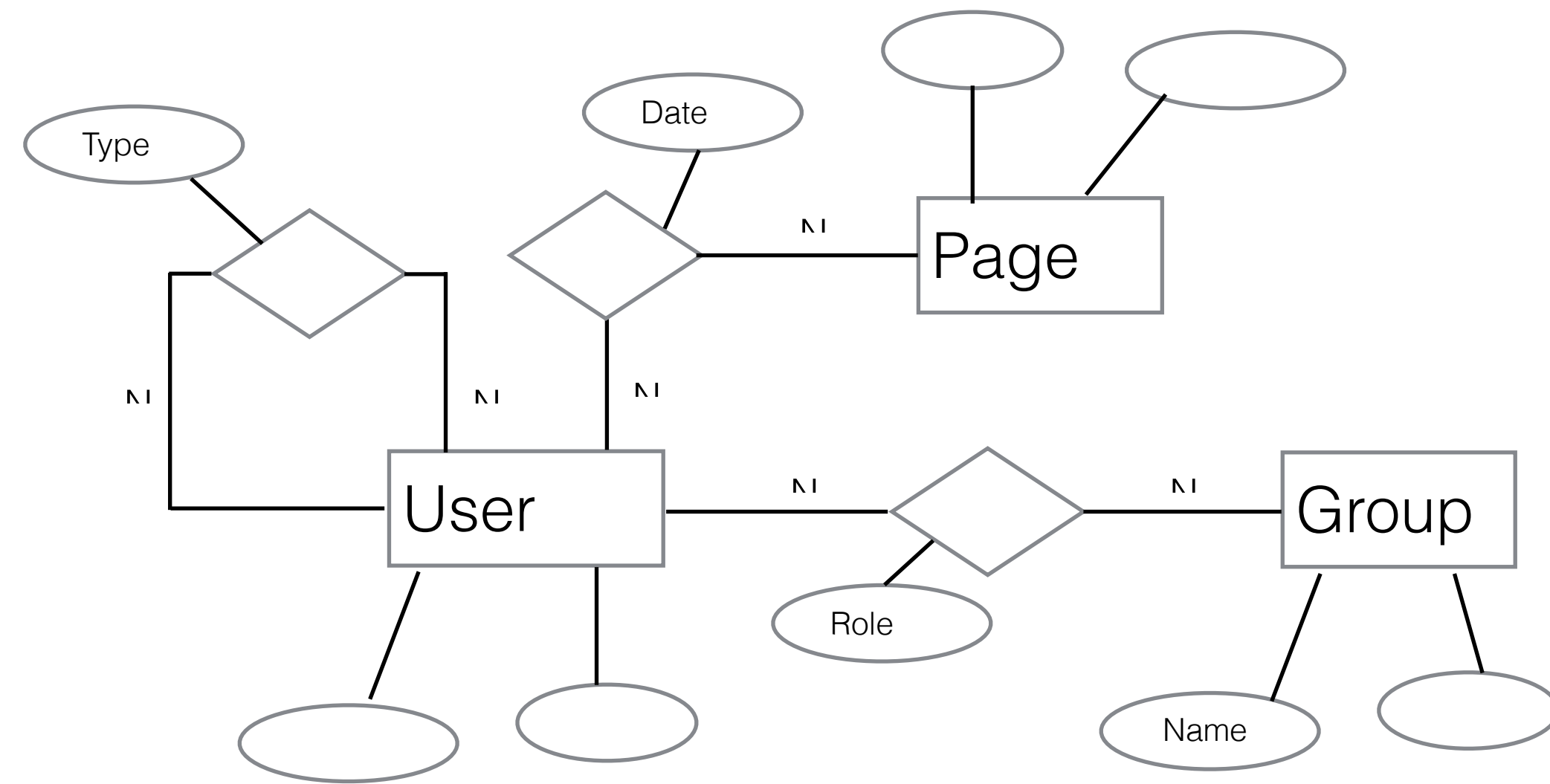
- looks reasonable!
- what you would expect
- **BUT!**

| | UserID | Username | PageID | Date | PageName | GroupID | Role | GroupName |
|--------|--------|----------|--------|--------|-----------|---------|-----------|-----------|
| | UI | John | P2 | 1.1.19 | Pizza | G2 | ADMIN | Geeks |
| | UI | John | P2 | 1.1.19 | Pizza | G4 | SUPPORTER | Travel |
| | UI | John | P2 | 1.1.19 | Pizza | G1 | TREASURER | Bikers |
| | UI | John | P2 | 1.1.19 | Pizza | G5 | CHIEF | MovieClub |
| UserID | UI | John | P1 | 1.4.19 | StarWars | G2 | ADMIN | Geeks |
| U1 | UI | John | P1 | 1.4.19 | StarWars | G4 | SUPPORTER | Travel |
| U2 | UI | John | P1 | 1.4.19 | StarWars | G1 | TREASURER | Bikers |
| U3 | UI | John | P1 | 1.4.19 | StarWars | G5 | CHIEF | MovieClub |
| | UI | John | P4 | 1.5.19 | VanGogh | G2 | ADMIN | Geeks |
| | UI | John | P4 | 1.5.19 | VanGogh | G4 | SUPPORTER | Travel |
| | UI | John | P4 | 1.5.19 | VanGogh | G1 | TREASURER | Bikers |
| | UI | John | P4 | 1.5.19 | VanGogh | G5 | CHIEF | MovieClub |
| | UI | John | P5 | 1.6.19 | Java | G2 | ADMIN | Geeks |
| | UI | John | P5 | 1.6.19 | Java | G4 | SUPPORTER | Travel |
| | UI | John | P5 | 1.6.19 | Java | G1 | TREASURER | Bikers |
| | UI | John | P5 | 1.6.19 | Java | G5 | CHIEF | MovieClub |
| | U2 | Mary | P3 | 1.2.19 | Liverpool | G1 | OWNER | Bikers |
| | U3 | Sarah | P1 | 1.3.19 | StarWars | G3 | FAN | Chefs |



We are stuck then?

- NO, there is a simple trick that can *fix* any database
- Always add a “bridge relation” to your set of tables
- This is a relation that contains the “superkey” of the whole database, i.e. the key of the Universal Relation
- This will capture the individuals that “tick all boxes”



Relations:

- $R1 = \{\underline{\text{UserID}}, \text{Username}\}$
- $R2 = \{\underline{\text{GroupID}}, \text{GroupName}\}$
- $R3 = \{\underline{\text{PageID}}, \text{PageName}\}$
- $R4 = \{\underline{\text{UserID}}, \underline{\text{PageID}}, \text{Date}\}$ (*user likes page*)
- $R5 = \{\underline{\text{UserID}}, \underline{\text{GroupID}}, \text{Role}\}$ (*user belongs to group*)
- $R6 = \{\underline{\text{UserID}}, \underline{\text{FriendID}}, \text{Type}\}$ (*user friends user*)
- **$R7 = \{\underline{\text{UserID}}, \underline{\text{GroupID}}, \underline{\text{PageID}}, \underline{\text{FriendID}}\}$ superkey**

Updated Tableaux test

| | UserID | Username | GroupID | GroupName | PageID | PageName | Date | Role | FriendID | Type |
|----|--------|----------|---------|-----------|--------|----------|--------|--------|----------|---------|
| R1 | Value1 | Value2 | | | | | | | | |
| R2 | | | Value3 | Value4 | | | | | | |
| R3 | | | | | Value5 | Value6 | | | | |
| R4 | Value1 | | | | Value3 | | Value7 | | | |
| R5 | Value1 | | Value3 | | | | | Value8 | | |
| R6 | Value1 | | | | | | | | Value9 | Value10 |
| R7 | Value1 | | Value3 | | Value3 | | | | Value9 | |

Updated Tableaux test



The bridge R7 will always guarantee the test is passed

| | UserID | Username | GroupID | GroupName | PageID | PageName | Date | Role | FriendID | Type |
|----|--------|----------|---------|-----------|--------|----------|--------|--------|----------|---------|
| R1 | Value1 | Value2 | | | | | | | | |
| R2 | | | Value3 | Value4 | | | | | | |
| R3 | | | | | Value5 | Value6 | | | | |
| R4 | Value1 | Value2 | | | Value5 | Value6 | Value7 | | | |
| R5 | Value1 | Value2 | Value3 | Value4 | | | | Value8 | | |
| R6 | Value1 | Value2 | | | | | | | Value9 | Value10 |
| R7 | Value1 | Value2 | Value3 | Value4 | Value5 | Value6 | Value7 | Value8 | Value9 | Value10 |

Updated counterexample

| | UserID | Username | GroupID | GroupName | PageID | PageName | Date | Role | FriendID | Type |
|----|--------|----------|---------|-----------|--------|-----------|--------|-----------|----------|------|
| R1 | U1 | John | G2 | Geeks | P2 | Pizza | 1.1.19 | Admin | .. | .. |
| R2 | U2 | Mary | G1 | Bikers | P3 | Liverpool | 1.2.19 | Owner | .. | .. |
| R3 | U3 | Sarah | G3 | Chefs | P1 | StarWars | 1.3.19 | Fan | .. | .. |
| R4 | U1 | John | G4 | Travel | P1 | StarWars | 1.4.19 | Supporter | .. | .. |
| R5 | U1 | John | G1 | Bikers | P4 | Van Gogh | 1.5.19 | Treasurer | .. | .. |
| R6 | U1 | John | G5 | MovieClub | P5 | Java! | 1.6.19 | Chief | ... | ... |
| R7 | U1 | John | G1 | Bikers | P1 | StarWars | 1.4.19 | Treasurer | ... | ... |



Ignore this for brevity

| | UserID | Username | GroupID | GroupName | PageID | PageName | Date | Role | Frie | Type |
|----|--------|----------|---------|-----------|--------|-----------|--------|-----------|------|------|
| R1 | U1 | John | G2 | Geeks | P2 | Pizza | 1.1.19 | Admin | .. | .. |
| R2 | U2 | Mary | G1 | Bikers | P3 | Liverpool | 1.2.19 | Owner | .. | .. |
| R3 | U3 | Sarah | G3 | Chefs | P1 | StarWars | 1.3.19 | Fan | .. | .. |
| R4 | U1 | John | G4 | Travel | P1 | StarWars | 1.4.19 | Supporter | .. | .. |
| R5 | U1 | John | G1 | Bikers | P4 | Van Gogh | 1.5.19 | Treasurer | .. | .. |
| R6 | U1 | John | G5 | MovieClub | P5 | Java! | 1.6.19 | Chief | ... | ... |
| R7 | U1 | John | G1 | Bikers | P1 | StarWars | 1.4.19 | Treasurer | .. | .. |

| UserID | Username |
|--------|----------|
| U1 | John |
| U2 | Mary |
| U3 | Sarah |

| GroupID | GroupName |
|---------|-----------|
| G1 | Bikers |
| G2 | Geeks |
| G3 | Chefs |
| G4 | Travel |
| G5 | MovieClub |

| PageID | PageName |
|--------|-----------|
| P1 | StarWars |
| P2 | Pizza |
| P3 | Liverpool |
| P4 | Van Gogh |
| P5 | Java! |

These are the users who both have a page and belong to a group, in all legal combinations

| UserID | GroupID | Role |
|--------|---------|-----------|
| U1 | G2 | Admin |
| U2 | G1 | Owner |
| U3 | G3 | Fan |
| U1 | G4 | Supporter |
| U1 | G1 | Treasurer |
| U1 | G5 | Chief |

| UserID | PageID | Date |
|--------|--------|--------|
| U1 | P2 | 1.1.19 |
| U2 | P3 | 1.2.19 |
| U3 | P1 | 1.3.19 |
| U1 | P1 | 1.4.19 |
| U1 | P4 | 1.5.19 |
| U1 | P5 | 1.6.19 |

| UserID | GroupID | PageID |
|--------|---------|--------|
| U1 | G2 | P2 |
| U2 | G1 | P3 |
| U3 | G3 | P1 |
| U1 | G4 | P1 |
| U1 | G1 | P4 |
| U1 | G5 | P5 |
| U1 | G1 | P1 |

| | UserID | Username | PageID | Date | PageName | GroupID | Role | GroupName |
|--------|--------|----------|--------|--------|-----------|---------|-----------|-----------|
| | UI | John | P2 | 1.1.19 | Pizza | G2 | ADMIN | Geeks |
| UserID | UI | John | P1 | 1.4.19 | StarWars | G4 | SUPPORTER | Travel |
| U2 | UI | John | P1 | 1.4.19 | StarWars | G1 | TREASURER | Bikers |
| U3 | UI | John | P4 | 1.5.19 | VanGogh | G1 | TREASURER | Bikers |
| | UI | John | P5 | 1.6.19 | Java | G5 | CHIEF | MovieClub |
| ⊗ | U2 | Mary | P3 | 1.2.19 | Liverpool | G1 | OWNER | Bikers |
| | U3 | Sarah | P1 | 1.3.19 | StarWars | G3 | FAN | Chefs |
| | | | | | | UI | GI | PI |



=

Conclusions

- We have gone full cycle (design wise at least)
 - from requirements to user stories
 - from user stories to conceptual design, in (E)ER
 - from conceptual design to logical design (in the relational model)
- we can identify issues and critical points in each of the phases, and we can express all of the above in a formal report
- Ready to go back to a more general notion of *quality* in CS/IT

